

## ANSWERS (AS 1 - Maths - Class 12 - 23.09.2025)

1	c) symmetric and transitive but not reflexive	11	c) $\pm 2\sqrt{2}$
2	b) injective only	12	a) $\tan x + \cot x + c$
3	d) $\frac{3\pi}{4}$	13	c) 110
4	b) $\frac{-1}{2}$	14	a) 1
5	a) -3	15	d) 0
6	d) 3	16	a) $\pm 3$
7	c) $-e^{y-x}$	17	D) skew-symmetric matrix
8	b) -y	18	b) $\tan^{-1}(x+1) + C$
9	b) 6 cm/s	19	(C) A is true but R is false
10	a) $\frac{1}{3}e^{x^3} + c$	20	(D) A is false and R is True
21	$CD - AB = 0 \Rightarrow CD = AB$ $AB = \begin{bmatrix} 2 & -1 \\ 3 & 4 \end{bmatrix} \cdot \begin{bmatrix} 5 & 2 \\ 7 & 4 \end{bmatrix} = \begin{bmatrix} 3 & 0 \\ 43 & 22 \end{bmatrix}$ $CD = AB = \begin{bmatrix} 3 & 0 \\ 43 & 22 \end{bmatrix}$	$\det(C) = (2)(8) - (5)(3) = 16 - 15 = 1$ $C^{-1} = \frac{1}{1} \cdot \begin{bmatrix} 8 & -5 \\ -3 & 2 \end{bmatrix} = \begin{bmatrix} 8 & -5 \\ -3 & 2 \end{bmatrix}$ $D = \begin{bmatrix} 8 & -5 \\ -3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 0 \\ 43 & 22 \end{bmatrix} \begin{bmatrix} -191 & -110 \\ 77 & 44 \end{bmatrix}$	
22	$\begin{aligned} & \frac{1}{\cos(x-a)\cos(x-b)} \\ &= \frac{1}{\sin(a-b)} \left[ \frac{\sin(a-b)}{\cos(x-a)\cos(x-b)} \right] \\ &= \frac{1}{\sin(a-b)} \left[ \frac{[\sin(x-b)\cos(x-a) - \cos(x-b)\sin(x-a)]}{\cos(x-a)\cos(x-b)} \right] \\ &= \frac{1}{\sin(a-b)} [\tan(x-b) - \tan(x-a)] \\ &= \frac{1}{\sin(a-b)} [-\log \cos(x-b)  + \log \cos(x-a) ] + \\ &= \frac{1}{\sin(a-b)} \left[ \log \left  \frac{\cos(x-a)}{\cos(x-b)} \right  \right] + C \end{aligned}$	$\begin{aligned} & \int \sqrt{x^2 + 2x + 5} dx = \int \sqrt{(x+1)^2 + 4} dx \\ & \text{Put } x+1 = y, \quad dx = dy. \\ & \int \sqrt{x^2 + 2x + 5} dx = \int \sqrt{y^2 + 2^2} dy \\ & \int \sqrt{x^2 + a^2} dx = \frac{1}{2} x \sqrt{x^2 + a^2} + \frac{a^2}{2} \log \left  x + \sqrt{x^2 + a^2} \right  + C \\ &= \frac{1}{2} y \sqrt{y^2 + 4} + \frac{4}{2} \log \left  y + \sqrt{y^2 + 4} \right  + C \\ &= \frac{1}{2} (x+1) \sqrt{x^2 + 2x + 5} + 2 \log \left  x+1 + \sqrt{x^2 + 2x + 5} \right  + C \end{aligned}$	
23		$\begin{aligned} & \sin^{-1}\left(\sin \frac{3\pi}{4}\right) + \cos^{-1}(\cos \pi) + \tan^{-1}(1) \\ &= \sin^{-1}\left(\sin \pi - \frac{\pi}{4}\right) + \cos^{-1}(\cos \pi) + \tan^{-1}\left(\frac{\pi}{4}\right) \\ &= \sin^{-1}\left(\sin \frac{\pi}{4}\right) + \pi + \frac{\pi}{4} \quad [\because \sin(\pi - \theta) = \sin \theta] \\ &= \frac{\pi}{4} + \pi + \frac{\pi}{4} \\ &= \frac{3\pi}{2} \end{aligned}$	
24	Reflexive: $a - a = 0$ , divisible by 2, $\forall a \in A$ $(a, a) \in R, \forall a \in A$ $\Rightarrow R$ is reflexive. <u>Symmetric</u> Let $(a, b) \in R \Rightarrow 2$ divides $a - b$ , say $a - b = 2m$ $\Rightarrow b - a = -2m \Rightarrow 2$ divides $b - a \Rightarrow (b, a) \in R \Rightarrow R$ is symmetric. <u>Transitive:</u> Let $(a, b), (b, c) \in R$ $\Rightarrow 2$ divides $a - b$ , say $a - b = 2m \Rightarrow 2$ divides $b - c$ , say $a - b = 2n$ $a - b + b - c = 2m + 2n$		

	<p><math>\Rightarrow a - c = 2(m + n) \Rightarrow 2 \text{ divides } a - c \Rightarrow R \text{ is Transitive.}</math></p> <p><math>\because R</math> is reflexive, symmetric and transitive</p> <p><math>\therefore R</math> is an equivalence relation.</p> <p><math>R = \{(a, b) : 2 \text{ divides } (a - b)\} \Rightarrow (a - b) \text{ is a multiple of } 2.</math></p> <p>So, <math>(a - 0)</math> is a multiple of 2 <math>\Rightarrow a</math> is a multiple of 2</p> <p>So, in set <math>Z</math> of integers, all the multiple of 2 will come in equivalence class <math>\{0\}</math></p> <p>Hence, equivalence class <math>\{0\} = \{2x\}</math> where <math>x = \text{integer } (Z).</math></p>	
25	$\frac{dy}{dx} = -\frac{b \sec^2 \theta}{a \sin \theta}$ $\frac{d}{d\theta} \left( -\frac{b \sec^2 \theta}{a \sin \theta} \right) = -\frac{(2b \sec^3 \theta \tan \theta)(a \sin \theta) - (b \sec^2 \theta)(a \cos \theta)}{(a \sin \theta)^2}$ $\frac{d^2y}{dx^2} = \frac{2ab \sec^3 \theta \tan \theta \sin \theta - ab \sec^2 \theta \cos \theta}{a^3 \sin^3 \theta}$ $\frac{d^2y}{dx^2} = \frac{\frac{8ab}{9} - \frac{2ab\sqrt{3}}{3}}{\frac{1}{8}a^3} = \left( \frac{8ab}{9} - \frac{2ab\sqrt{3}}{3} \right) \cdot \frac{8}{a^3} = \frac{8b}{a^2} \cdot \frac{8 - 6\sqrt{3}}{9}$	$\sec^2 \theta = \left( \frac{2}{\sqrt{3}} \right)^2 = \frac{4}{3}$ $\sec^3 \theta = \left( \frac{2}{\sqrt{3}} \right)^3 = \frac{8}{3\sqrt{3}}$ $\tan \theta = \frac{1}{\sqrt{3}}$ $\sin \theta = \frac{1}{2}$ $\cos \theta = \frac{\sqrt{3}}{2}$
26	$y\sqrt{1-x^2} + x\sqrt{1-y^2} = 1$ $\frac{dy}{dx} \cdot \sqrt{1-x^2} - \frac{xy}{\sqrt{1-x^2}} + \sqrt{1-y^2} - \frac{xy}{\sqrt{1-y^2}} \cdot \frac{dy}{dx} = 0$ $\frac{dy}{dx} \left( \sqrt{1-x^2} - \frac{xy}{\sqrt{1-y^2}} \right) = \frac{xy}{\sqrt{1-x^2}} - \sqrt{1-y^2}$ $\frac{dy}{dx} = \frac{\frac{xy}{\sqrt{1-x^2}} - \sqrt{1-y^2}}{\sqrt{1-x^2} - \frac{xy}{\sqrt{1-y^2}}}$ $\frac{dy}{dx} = -\sqrt{\frac{1-y^2}{1-x^2}}$	
27	<p>Let <math>I = \int 1 \cdot \tan^{-1} x dx</math></p> $I = \tan^{-1} x \int 1 dx - \int \left\{ \left( \frac{d}{dx} \tan^{-1} x \right) \int 1 \cdot dx \right\} dx$ $= \tan^{-1} x \cdot x - \int \frac{1}{1+x^2} \cdot x dx$ $= x \tan^{-1} x - \frac{1}{2} \int \frac{2x}{1+x^2} dx$ $= x \tan^{-1} x - \frac{1}{2} \log 1+x^2  + C$ $= x \tan^{-1} x - \frac{1}{2} \log(1+x^2) + C$ $\tan^{-1} x = x \tan^{-1} x - \frac{1}{2} \log(1+x^2) + C$	$e^x \left( \frac{1+\sin x}{1+\cos x} \right) = e^x \left( \frac{\sin^2 \left( \frac{x}{2} \right) + \cos^2 \left( \frac{x}{2} \right) + 2 \sin \frac{x}{2} \cdot \cos \frac{x}{2}}{2 \cos^2 \left( \frac{x}{2} \right)} \right)$ $= e^x \left( \frac{\left( \sin \frac{x}{2} + \cos \frac{x}{2} \right)^2}{2 \cos^2 \left( \frac{x}{2} \right)} \right) = \frac{e^x}{2} \left( \frac{\sin \frac{x}{2} + \cos \frac{x}{2}}{\cos \frac{x}{2}} \right)^2$ $= \frac{e^x}{2} \left( \tan \frac{x}{2} + 1 \right)^2 = \frac{e^x}{2} \left( \tan^2 \frac{x}{2} + 1 + 2 \tan \frac{x}{2} \right)$ $e^x \left( \frac{1+\sin x}{1+\cos x} \right) = \frac{e^x}{2} \left( \sec^2 \frac{x}{2} + 2 \tan \left( \frac{x}{2} \right) \right)$ $= e^x \left( \tan \left( \frac{x}{2} \right) + \frac{1}{2} \sec^2 \left( \frac{x}{2} \right) \right)$ $\int e^x \left( \frac{1+\sin x}{1+\cos x} \right) dx = \int e^x \left( \tan \left( \frac{x}{2} \right) + \frac{1}{2} \sec^2 \left( \frac{x}{2} \right) \right) dx$ $\int e^x \left( \frac{1+\sin x}{1+\cos x} \right) dx = e^x \tan \frac{x}{2} + C$

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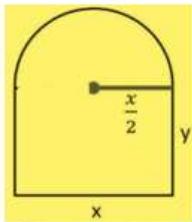
Let Length of rectangle be  $x$  & breadth of rectangle be  $y$   
Diameter of semicircle =  $x \Rightarrow$  Radius of semicircle =  $\frac{x}{2}$

Perimeter of window = 10 m

$$x + 2y + \pi\left(\frac{x}{2}\right) = 10$$

$$2y = 10 - x - \frac{\pi x}{2}$$

$$y = 5 - x\left(\frac{1}{2} + \frac{\pi}{4}\right)$$



$$\text{Putting } \frac{dA}{dx} = 0 \Rightarrow 0 = 5 - x - \frac{\pi x}{4}$$

$$x + \frac{\pi x}{4} = 5 \Rightarrow \left(1 + \frac{\pi}{4}\right)x = 5$$

$$x = \frac{20}{\pi + 4}$$

$$\frac{d^2A}{dx^2} = \frac{d\left(5 - x - \frac{\pi x}{4}\right)}{dx} = -1 - \frac{\pi}{4} < 0$$

$$\frac{d^2A}{dx^2} < 0 \text{ at } x = \frac{20}{\pi + 4}; \text{ A is maximum when } x = \frac{20}{\pi + 4}$$

$$y = 5 - x\left(\frac{1}{2} + \frac{\pi}{4}\right) = 5 - \frac{20}{\pi + 4}\left(\frac{1}{2} + \frac{\pi}{4}\right) \Rightarrow y = \frac{10}{\pi + 4}$$

Hence, for maximum area,

$$\text{Length} = x = \frac{20}{\pi + 4} \text{ m & Breadth} = y = \frac{10}{\pi + 4} \text{ m}$$

- OR -

$$V = x^2y \quad \dots \text{(i)}$$

$$S = x^2 + 4xy \quad \dots \text{(ii)}$$

$$\text{On putting } y = \frac{V}{x^2} \quad S = x^2 + 4x \cdot \frac{V}{x^2}$$

On differentiating both side w.r.t  $x$ , we get

$$\frac{dS}{dx} = 2x - \frac{4V}{x^2}$$

$$\text{put } \frac{dS}{dx} = 0$$

$$2x - \frac{4V}{x^2} = 0$$

$$2y = x \text{ or } y = \frac{x}{2}$$

$$\text{Also, } \frac{d^2S}{dx^2} = \frac{d}{dx}\left(\frac{dS}{dx}\right) = \frac{d}{dx}\left(2x - \frac{4V}{x^2}\right) = 2 + \frac{8y}{x} > 0,$$

or  $S$  is minimum. Hence, total surface area of the tank is least, when depth is half of its width

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$$f(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad f(\beta) = \begin{bmatrix} \cos \beta & -\sin \beta & 0 \\ \sin \beta & \cos \beta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} \cos \beta & -\sin \beta & 0 \\ \sin \beta & \cos \beta & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos \alpha \cos \beta - \sin \alpha \sin \beta & -\cos \alpha \sin \beta - \sin \alpha \cos \beta & 0 \\ \sin \alpha \cos \beta + \cos \alpha \sin \beta & -\sin \alpha \sin \beta + \cos \alpha \cos \beta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$f(\alpha) \cdot f(\beta) = \begin{bmatrix} \cos(\alpha + \beta) & -\sin(\alpha + \beta) & 0 \\ \sin(\alpha + \beta) & \cos(\alpha + \beta) & 0 \\ 0 & 0 & 1 \end{bmatrix} = f(\alpha + \beta)$$

$$\cos \alpha \cos \beta - \sin \alpha \sin \beta = \cos(\alpha + \beta)$$

$$\sin \alpha \cos \beta + \cos \alpha \sin \beta = \sin(\alpha + \beta)$$

$$A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$$

$$LHS = A^2 - 5A + 7I$$

$$= \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} - 5 \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} + 7 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 9 - 1 & 3 + 2 \\ -3 - 2 & -1 + 4 \end{bmatrix} - \begin{bmatrix} 15 & 5 \\ -5 & 10 \end{bmatrix} + \begin{bmatrix} 7 & 0 \\ 0 & 7 \end{bmatrix}$$

$$= \begin{bmatrix} 8 - 15 + 7 & 5 - 5 + 0 \\ -5 + 5 + 0 & 3 - 10 + 7 \end{bmatrix}$$

$$= \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} = O = RHS$$

$$\Rightarrow A^2 - 5A + 7I = 0 \Rightarrow AI - 5I = -7A^{-1}$$

$$\Rightarrow 7A^{-1} = 5I - A = 5 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 5 & 0 \\ 0 & 5 \end{bmatrix} - \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix} = \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix}$$

$$\Rightarrow A^{-1} = \frac{1}{7} \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix}$$

30	$A = \begin{bmatrix} 2 & -2 & -4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{bmatrix} \quad A^T = \begin{bmatrix} 2 & -1 & 1 \\ -2 & 3 & -2 \\ -4 & 4 & -3 \end{bmatrix}$ $A + A^T = \begin{bmatrix} 2+2 & -2+(-1) & -4+1 \\ -1+(-2) & 3+3 & 4+(-2) \\ 1+(-4) & -2+4 & -3+(-3) \end{bmatrix} = \begin{bmatrix} 4 & -3 & -3 \\ -3 & 6 & 2 \\ -3 & 2 & -6 \end{bmatrix}$ $S = \frac{1}{2} \begin{bmatrix} 4 & -3 & -3 \\ -3 & 6 & 2 \\ -3 & 2 & -6 \end{bmatrix} = \begin{bmatrix} 2 & -1.5 & -1.5 \\ -1.5 & 3 & 1 \\ -1.5 & 1 & -3 \end{bmatrix}$ $A - A^T = \begin{bmatrix} 2-2 & -2-(-1) & -4-1 \\ -1-(-2) & 3-3 & 4-(-2) \\ 1-(-4) & -2-4 & -3-(-3) \end{bmatrix} = \begin{bmatrix} 0 & -1 & -5 \\ 1 & 0 & 6 \\ 5 & -6 & 0 \end{bmatrix}$ $K = \frac{1}{2} \begin{bmatrix} 0 & -1 & -5 \\ 1 & 0 & 6 \\ 5 & -6 & 0 \end{bmatrix} = \begin{bmatrix} 0 & -0.5 & -2.5 \\ 0.5 & 0 & 3 \\ 2.5 & -3 & 0 \end{bmatrix}$	
31	$f(x) = \frac{x^4}{4} - x^3 - 5x^2 + 24x + 12$ $f'(x) = x^3 - 3x^2 - 10x + 24$ $f'(x) = (x-2)(x-4)(x+3)$	<p><math>f(x)</math> is increasing when <math>f'(x) &gt; 0</math>:</p> <ul style="list-style-type: none"> <li>On intervals: <math>(-3, 2) \cup (4, \infty)</math></li> </ul> <p><math>f(x)</math> is decreasing when <math>f'(x) &lt; 0</math>:</p> <ul style="list-style-type: none"> <li>On intervals: <math>(-\infty, -3) \cup (2, 4)</math></li> </ul>
32	$A = \begin{bmatrix} 1 & 1 & 1 \\ 4 & 3 & 2 \\ 6 & 2 & 3 \end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, \quad B = \begin{bmatrix} 21 \\ 60 \\ 70 \end{bmatrix}$ $\det(A) = 1(3 \cdot 3 - 2 \cdot 2) - 1(4 \cdot 3 - 2 \cdot 6) + 1(4 \cdot 2 - 3 \cdot 6)$ $= 1(9 - 4) - 1(12 - 12) + 1(8 - 18)$ $= 1(5) - 1(0) + 1(-10)$ $= 5 - 0 - 10$ $= -5$	$\text{adj}(A) = \begin{bmatrix} 5 & -1 & -1 \\ 0 & -3 & 2 \\ -10 & 4 & -1 \end{bmatrix}$ $X = \frac{1}{-5} \begin{bmatrix} 5 & -1 & -1 \\ 0 & -3 & 2 \\ -10 & 4 & -1 \end{bmatrix} \cdot \begin{bmatrix} 21 \\ 60 \\ 70 \end{bmatrix} = \begin{bmatrix} -25 \\ -40 \\ -40 \end{bmatrix}$ $X = \begin{bmatrix} -25 \div -5 \\ -40 \div -5 \\ -40 \div -5 \end{bmatrix} = \begin{bmatrix} 5 \\ 8 \\ 8 \end{bmatrix}$
33	$f(x) = \sqrt{16 - x^2}$ $x = 2, f(x) = \sqrt{12} \quad x = -2, f(x) = \sqrt{12}$ <p>Since, for <math>x = 2</math> and <math>-2</math>, the function has same image  <math>\therefore</math> The given function is not one-one.</p> $y = \sqrt{16 - x^2}$ $y^2 = 16 - x^2$ $x = \sqrt{16 - y^2} \quad (4-y)(4+y) \geq 0$ 	<p>' For every <math>y \in [0, 4]</math> <math>\exists x \in [-4, 4]</math> such that <math>y = f(x)</math></p> <p>' The given function is onto</p> $f(a) = \sqrt{12}$ $\sqrt{16 - y^2} = \sqrt{7}$ $16 - a^2 = 7$ $a^2 = 9$ $a = \pm 3$
34	<p>Given that <math>y = Ae^{mx} + Be^{nx}</math>, therefore,</p> $\frac{dy}{dx} = \frac{d}{dx}(Ae^{mx} + Be^{nx}) = mAe^{mx} + nBe^{nx}$ $\Rightarrow \frac{d^2y}{dx^2} = \frac{d}{dx}(mAe^{mx} + nBe^{nx}) = m^2Ae^{mx} + n^2Be^{nx}$ $\text{LHS} = (m^2Ae^{mx} + n^2Be^{nx}) - (m+n)(mAe^{mx} + nBe^{nx}) + mny$ $= m^2Ae^{mx} + n^2Be^{nx} - (m^2Ae^{mx} + mnBe^{nx} + mnAe^{mx} + n^2Be^{nx}) + mny$ $= -(mnAe^{mx} + mnBe^{nx}) + mny = -mn(Ae^{mx} + Be^{nx}) + mny = -mny + mny = 0 = \text{RHS}$	

34 OR	$u = (\log x)^x \quad \frac{du}{dx} = u \left[ \frac{1}{\log x} + \log(\log x) \right] = (\log x)^x \left[ \frac{1}{\log x} + \log(\log x) \right]$ $v = x^{\log x} \quad \frac{1}{v} \frac{dv}{dx} = 2 \log x \frac{d}{dx} (\log x) = 2 \log x \times \frac{1}{x} \quad \Rightarrow \frac{dv}{dx} = v \left[ \frac{2 \log x}{x} \right] = x^{\log x} \left[ \frac{2 \log x}{x} \right]$ $\frac{dy}{dx} = (\log x)^x \left[ \frac{1}{\log x} + \log(\log x) \right] + x^{\log x} \left[ \frac{2 \log x}{x} \right]$ $\Rightarrow \frac{dy}{dx} = (\log x)^{x-1} [1 + \log x \log(\log x)] + 2x^{\log x-1} \cdot \log x$
35	<p>Let <math>5x - 2 = A \frac{d}{dx}(1 + 2x + 3x^2) + B</math></p> $\Rightarrow 5x - 2 = A(2 + 6x) + B$ $5 = 6A \Rightarrow A = \frac{5}{6}$ $2A + B = -2 \Rightarrow B = -\frac{11}{3}$ $\therefore 5x - 2 = \frac{5}{6}(2 + 6x) + \left(-\frac{11}{3}\right)$ $\Rightarrow \int \frac{5x - 2}{1 + 2x + 3x^2} dx = \int \frac{\frac{5}{6}(2 + 6x) - \frac{11}{3}}{1 + 2x + 3x^2} dx$ $= \frac{5}{6} \int \frac{2 + 6x}{1 + 2x + 3x^2} dx - \frac{11}{3} \int \frac{1}{1 + 2x + 3x^2} dx$ <p><math>I_1 = \int \frac{2 + 6x}{1 + 2x + 3x^2} dx</math>  <math>I_1 = \log 1 + 2x + 3x^2 </math></p> <p><math>I_2 = \int \frac{1}{1+2x+3x^2} dx</math>  <math>I_2 = \frac{1}{3} \int \frac{1}{\left(x+\frac{1}{3}\right)^2 + \left(\frac{\sqrt{2}}{3}\right)^2} dx</math>  <math>= \frac{1}{3} \left[ \frac{1}{\frac{\sqrt{2}}{3}} \tan^{-1} \left( \frac{x+\frac{1}{3}}{\frac{\sqrt{2}}{3}} \right) \right] = \frac{1}{3} \left[ \frac{3}{\sqrt{2}} \tan^{-1} \left( \frac{3x+1}{\sqrt{2}} \right) \right]</math></p> <p><math>\int \frac{5x - 2}{1 + 2x + 3x^2} dx</math>  <math>= \frac{5}{6} \log 1 + 2x + 3x^2  - \frac{11}{3\sqrt{2}} \tan^{-1} \left( \frac{3x+1}{\sqrt{2}} \right) + C</math></p>
<p>Let <math>t = x^2</math></p> $\frac{(x^2+1)(x^2+2)}{(x^2+3)(x^2+4)} = \frac{(t+1)(t+2)}{(t+3)(t+4)}$ $= \frac{t^2 + 3t + 2}{t^2 + 7t + 12}$ $\frac{t^2 + 3t + 2}{t^2 + 7t + 12} = 1 + \frac{-4t - 10}{t^2 + 7t + 12}$ $= 1 + \frac{-(4t + 10)}{(t+3)(t+4)}$ $\frac{4t + 10}{(t+3)(t+4)} = \frac{A}{(t+3)} + \frac{B}{(t+4)}$ $\frac{4t + 10}{(t+3)(t+4)} = \frac{A(t+4) + B(t+3)}{(t+3)(t+4)}$ $4t - 10 = A(t+4) + B(t+3)$ <p style="color: red;">→ <math>A = -2 \quad B = 6</math></p>	$\frac{4t + 10}{(t+3)(t+4)} = \frac{-2}{(t+3)} + \frac{6}{(t+4)}$ $\frac{4x^2 - 10}{(x^2+3)(x^2+4)} = \frac{-2}{(x^2+3)} + \frac{6}{(x^2+4)}$ $\int \frac{(x^2+1)(x^2+2)}{(x^2+3)(x^2+4)} = \int 1 - \left[ \frac{-2}{(x^2+3)} + \frac{6}{(x^2+4)} \right] dx$ $= \int 1 \cdot dx + \int \frac{2}{(x^2+3)} dx - \int \frac{6}{(x^2+4)} dx$ $= \int 1 \cdot dx + 2 \int \frac{1}{x^2 + (\sqrt{3})^2} dx - 6 \int \frac{1}{(x^2+2^2)} dx$ $= x + 2 \times \frac{1}{\sqrt{3}} \tan^{-1} \frac{x}{\sqrt{3}} - 6 \times \frac{1}{2} \tan^{-1} \frac{x}{2} + C$ $= x + \frac{2}{\sqrt{3}} \tan^{-1} \left( \frac{x}{\sqrt{3}} \right) - 3 \tan^{-1} \left( \frac{x}{2} \right) + C$
36	<p><b>1. Symmetric Relation:</b>          A relation <math>R</math> on a set <math>A</math> is symmetric if for every <math>(a, b) \in R, (b, a) \in R</math>.</p> <p><b>Checking Symmetry:</b></p> <ul style="list-style-type: none"> <li>● Given <math>(l_1, l) \in R</math> <math>l</math> implies <math>l</math> is parallel to <math>l_1</math>.</li> <li>● Parallelism is symmetric: If <math>l</math> is parallel to <math>l_2</math>, then <math>l_2</math> is also parallel to <math>l</math>.</li> <li>● Hence, <math>(l_2, l_1) \in R</math> whenever <math>(l_1, l_2) \in R</math>.</li> </ul> <p>Therefore, the relation <math>R</math> is symmetric.</p>

	<p><b>Set of Rail Lines Related to the Given Line:</b>          If one of the rail lines on the railway track is represented by the equation <math>y = 3x + 2</math>, we need to find the set of rail lines in <math>R</math> related to it.</p> <p><b>Equation of the Given Line:</b>          ● The given line is <math>y = 3x + 2</math>.</p> <p><b>Finding Related Lines:</b></p> <ul style="list-style-type: none"> <li>● Lines related to this one are parallel lines with the same slope, which is <math>3</math>.</li> <li>● The general equation of lines parallel to <math>y = 3x + 2</math> is <math>y = 3x + c</math>, where <math>c</math> is any real number.</li> </ul> <p>Therefore, the set of rail lines in <math>R</math> related to <math>y = 3x + 2</math> is:  <math>\{y = 3x + c \mid c \in R\}</math></p>		
37	$F = \frac{40^2}{500} - \frac{40}{4} + 14$ $F = \frac{1600}{500} - 10 + 14$ $F = 3.2 - 10 + 14$ $F = 7.2$ $\frac{dF}{dV} = \frac{d}{dV} \left( \frac{V^2}{500} - \frac{V}{4} + 14 \right)$ $\frac{dF}{dV} = \frac{2V}{500} - \frac{1}{4}$ $\frac{dF}{dV} = \frac{V}{250} - \frac{1}{4}$	$\frac{V}{250} - \frac{1}{4} = 0$ $\frac{V}{250} = \frac{1}{4}$ $V = \frac{250}{4}$ $V = 62.5$	<p>Given:</p> $\frac{V}{250} - \frac{1}{4} = -0.01$ $V = 60$ <p>Now, find <math>F</math> when <math>V = 60</math>:</p> $F = \frac{60^2}{500} - \frac{60}{4} + 14$ $F = 6.2$ <p>Fuel required = <math>\frac{6.2}{100} \times 600</math></p> <p>Fuel required = <math>6.2 \times 6</math></p> <p>Fuel required = 37.2</p>
38	$3x - 5y = 15000$ $4x - 7y = 15000$ $\begin{bmatrix} 3 & -5 \\ 4 & -7 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 15000 \\ 15000 \end{bmatrix}$ $A^{-1} = \frac{1}{-1} \begin{bmatrix} -7 & 5 \\ -4 & 3 \end{bmatrix} = \begin{bmatrix} 7 & -5 \\ 4 & -3 \end{bmatrix}$	$x = 30000 \text{ & } y = 15000$ <p><b>Monthly income of Rita</b> = ₹<math>3x</math> = ₹<math>3 \times 30,000</math> = ₹<b>90,000</b></p> <p><b>Monthly income of Ritika</b> = ₹<math>4x</math> = ₹<math>4 \times 30,000</math> = ₹<b>1,20,000</b></p>	